## Enhanced spin susceptibility in phosphorus-doped silicon

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(Received 17 May 1988)

The influence of the many-valley isotropic effect of the conduction band with a variational  $N_d$  dependence on the metal-nonmetal transition of doped semiconductors is investigated further in the calculation of spin susceptibility. A previously developed Gutzwiller method for finite temperature is used. Good agreement with experimental findings is found.

Work to date has concentrated much effort on spin susceptibility  $\chi_s$  around the metal-nonmetal transition critical point  $N_c$  in Si:P.<sup>1</sup> Above  $N_c$ , there are up to now the data<sup>2</sup> of Quirt and Marko and the calculation<sup>3</sup> of Chao and Berggren (CB) which show clearly the temperature and donor concentration dependence  $N_D$  on  $\chi_s$ .

In recent works<sup>4</sup> I have shown the influence of the many-valley isotropic effect of the conduction band with a variational  $N_D$  dependence of the wave function on the metal-nonmetal transition of doped semiconductors. In this report I show that such a scheme, to some extent,

has a remarkable effect on  $\chi_s$  of Si:P when it is used in the CB approach, which is an extension of the Gutzwiller method for finite temperature. The  $\chi_s$  obtained is written as

$$\chi_s(T) = \eta_{\chi}(T)\chi_0(T) , \qquad (1)$$

where  $\eta_{\chi}$  is an enhancement factor and  $\chi_0$  is the Pauli spin susceptibility.<sup>3</sup> CB have used an anisotropic wave function and adjusted the intradonor Coulomb interac-



FIG. 1.  $\chi_s$  as a function of  $N_D$ . Inset for T = 1.1 K;  $\Box$ , Ref. 1; +, Ref. 2;  $\bigcirc$ , Ref. 12; ----, present work.

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tion or correlation energy<sup>5-7</sup> U in order to get the experimental  $N_c$ . Here the calculation for  $\chi_s$  is performed, in the wake of the CB approach, but for the experimental U within the former above scheme.<sup>4,8,9</sup> In Fig. 1 a reasonable fitting with experimental data<sup>2</sup> found for  $\chi_s$  is shown as a function of  $N_D$ . From the metallic side, metalnonmetal transition takes place when the number of dou-

- <sup>1</sup>D. F. Holcomb, in *Localization and Interaction in Disordered Metals and Doped Semiconductors*, edited by D. M. FinLayson (Scottish Universities Summer School in Physics, Edinburgh, 1986), p. 313.
- <sup>2</sup>J. D. Quirt and J. R. Mako, Phys. Rev. B 5, 1716 (1972); 7, 3842 (1973).
- <sup>3</sup>K. A. Chao and K.-F. Berggren, Phys. Rev. Lett. **34**, 880 (1975).
- <sup>4</sup>A. Ferreira da Silva, Phys. Rev. Lett. **59**, 1263 (1987); Phys. Rev. B **37**, 4799 (1988).
- <sup>5</sup>J. Hubbard, Proc. R. Soc. London, Ser. A **276**, 238 (1963); **281**, 401 (1964).
- <sup>6</sup>The correlation energy U in the isotropic case of hydrogen donor gives  $U \simeq 0.63e^2/\kappa a$ , where  $\kappa$  is the dielectric constant

bly occupied sites is zero. I find  $N_c = 3.5 \times 10^{18}$  cm<sup>-3</sup> while the experiment is  $3.7 \times 10^{18}$  cm<sup>-3</sup>.<sup>10</sup> I also show, in the inset, the results of  $\chi_s$  for 1.1 K, as well as its dependence on U.<sup>11</sup> The  $\chi_s$  shows good agreement when compared to the available experimental data.<sup>2,12</sup> I expect that such results may motivate in the future a more thorough treatment along the concentration region presented.

and a the donor wave-function radius.

- <sup>7</sup>See, e.g., J. C. Slater, Quantum Theory of Molecules and Solids (McGraw-Hill, New York, 1968), Vol. I, p. 58.
- <sup>8</sup>M. Taniguchi and S. Narita, J. Phys. Soc. Jpn. 43, 1262 (1977).
- <sup>9</sup>The experimental value of U is  $U \simeq 0.96E_D$  ( $E_D$  being the ionization energy of the system considered). The ratio  $U/E_D$  is rather insensitive to mass anisotropic (cf. Ref. 8).
- <sup>10</sup>T. F. Rosenbaum, K. Andres, G. A. Thomas, and R. N. Bhatt, Phys. Rev. Lett. **45**, 1723 (1980).
- <sup>11</sup>That is in effect an enhancement of  $\chi_s$  due to U. The values of U are obtained from Refs. 6 and 9, and a lower value of them is used for the sake of comparison.
- <sup>12</sup>S. Ikehata and S. Kobayashi, Solid State Commun. 56, 607 (1985).