

Elastic and absorption cross sections for electron–hydroxyl radical collisions

A. M. C. Sobrinho

*Departamento de Física, UFSCar 13565-905, São Carlos, SP, Brazil
and Departamento de Física de Estado Sólido, UFBA 40170-290, Salvador, BA, Brazil*

N. B. H. Lozano and M.-T. Lee

Departamento de Química, UFSCar 13565-905 São Carlos, SP, Brazil

(Received 30 March 2004; published 28 September 2004)

In this work, we report a theoretical study on electron collisions with OH radicals in the low and intermediate energy ranges. Calculated elastic differential, integral, and momentum-transfer cross sections as well as grand-total (elastic + inelastic) and total absorption cross sections for electron-OH collisions are reported in the 1–500-eV range. A complex optical potential composed by static, exchange, correlation-polarization plus absorption contributions, derived from a fully molecular wave function, is used to describe the interaction dynamics. The Schwinger variational iterative method combined with the distorted-wave approximation is applied to calculate scattering amplitudes. Present calculated results are compared with the existing data for electron-OH scattering in the literature. Also, comparison made between our calculated cross sections for elastic scattering with the theoretical and experimental results for electron-H₂O collisions has revealed remarkable similarity even at incident energies as low as 2 eV.

DOI: 10.1103/PhysRevA.70.032717

PACS number(s): 34.80.Bm

I. INTRODUCTION

Cross sections for electron scattering from a variety of molecules and free radicals are demanded in different fields of the pure and applied sciences [1–3]. In particular, interest in electron collisions with reactive radicals has grown recently [4–8], in view of their important role in physical and chemical processes involved in a number of applications such as lasers [9], gas discharges, plasmas [10], etc., as well as in the atmospheric and astrophysical studies [11]. The hydroxyl (OH) is one of such radicals. The OH radicals can be produced in Earth's atmosphere by vuv photolysis of water [12]. Due to its high reactivity, OH is an important reaction intermediate in the atmospheric chemistry [13–16]. The OH radicals have also been identified in the extreme carbon star IRC+10216 [17] as well as in the comets Hale-Bopp [18] and C/1999 HI(Lee) [19]. Moreover, OH plays an important role in biology and medicine. It is well known that the nuclear radiation that penetrates into the human body may cause several types of cancer. The OH radicals are pointed out as a precursor of this disease because it may cause damages in cells [20–23]. In the human body, OH is formed by the interaction of the water molecule and secondary electrons with appreciable kinetic energy, which are produced by nuclear radiation [24].

Because of its relevant application in a number of fields, the knowledge of the electron-OH collisional dynamics is certainly of interest. However, there is a lack of either experimental or theoretical studies on such matter in the literature. Due to its high chemical reactivity, it would be very difficult to generate a OH radical beam to be interacted with electron beam, thus experimental studies on electron-OH collisions would be a very hard task. To our knowledge, there is only one article [25] that reports the measurement of

total ionization cross sections (TICS's) for electron-OH collisions. Theoretically, studies for electron-OH scattering are equally scarce. Low-energy electron scattering from the ground electron state (²Π) of OH was investigated by Chen and Morgan [26] using the *R*-matrix method. In that work, they reported calculated cross sections for the 0→1 vibrational transition of OH by electron impact in the 0–3-eV energy range as well as the differential cross sections (DCS's) for elastic *e*⁻-OH scattering at a single incident energy of 1.58 eV. Also, Joshipura *et al.* [5] have calculated total cross sections (TCS's) and total absorption cross sections (TACS's), and estimated TICS's for electron-OH collisions in the 10–2000-eV range. A complex optical potential for electron-atom interaction combined with the additivity rule was used in their calculations. Although this method may provide reliable cross sections for incident energies above 100 eV, it is expected to fail at lower energies. In this work, we present a theoretical study on electron-OH scattering covering a wide incident energy range. More specifically, DCS's, integral (ICS's) and momentum transfer (MTCS's) cross sections for elastic *e*⁻-OH scattering as well as TCS's and TACS's in the 1–500-eV energy range are calculated and reported. The present study made use of a complex optical potential to represent the electron-radical interaction, whereas a combination of the Schwinger variational iterative method (SVIM) [27,28] and the distorted-wave approximation (DWA) [29–31] is used to solve the scattering equations. This procedure has already been applied to treat electron scattering by a number of molecules [32–35] and radicals [6–8] and has provided reliable DCS's, ICS's, and MTCS's over a wide energy range.

The organization of this paper is as follows. In Sec. II, we describe briefly the theory used and also some details of the calculation. In Sec. III we present our calculated results.

II. THEORY AND CALCULATION

Details of the SVIM [27,28] and the DWA [29–31] have already been presented previously, and will only be outlined here. Within the fixed-nuclei framework, the electron-molecule scattering dynamics is represented by a complex optical potential,

$$V_{opt}(\vec{r}) = V^{SEP}(\vec{r}) + iV_{ab}(\vec{r}), \quad (1)$$

where the V^{SEP} is the real part of the interaction potential composed by the static (V_{st}), the exchange (V_{ex}), and the correlation-polarization contributions (V_{cp}) whereas V_{ab} is the absorption potential. In our calculation, V_{st} and V_{ex} are derived exactly from a restricted open-shell Hartree-Fock (ROHF) self-consistent-field (SCF) target wave function. A parameter-free model potential introduced by Padial and Norcross [36] is used to account for the correlation-polarization contributions. In this model, a short-range correlation potential between the scattering and target electrons is defined in an inner interaction region and a long-range polarization potential in an outer region. The first crossing of the correlation and polarization potential curves defines the inner and outer regions. The short-range correlation potential is derived using the target electronic density according to Eq. (9) of Padial and Norcross [36]. In addition, an asymptotic form of the polarization potential is used for the long-range electron-target interactions. The model potential of Padial and Norcross is in fact rather crude. Specifically, the use of the free-electron-gas approximation in the inner region may not reflect realistically the properties of targets. Also, the junction of the potentials calculated separately in the inner and outer regions is somehow arbitrary. Despite that, the simplicity of this model makes it quite useful in theoretical studies of electron scattering by atoms and molecules. Moreover, V_{cp} generated by this model has the correct asymptotic form of polarization potential which is very interesting for low-energy electron-molecule scattering, due to the low penetration capacity of these electrons into targets. The application of this model requires dipole polarizabilities to generate the asymptotic form of V_{cp} . Since there is no experimental and/or theoretical values available in the literature for the OH radical, they were calculated in this work at ROHF level of approximation. The calculated values are $\alpha_{zz}=7.885$ a.u. and $\alpha_{xx}=5.942$ a.u. No cutoff or other adjusted parameters are needed in the calculation of V_{cp} .

Although the main features of the absorption effects are known, taking these effects into account in an *ab initio* treatment of electron-molecule scattering is very difficult. Presently, despite the *ab initio* methods (e.g., R matrix [37], Kohn variational [38], and Schwinger multichannel [39], etc.) are routinely applied to electron-molecule collisional studies, these applications are in general limited in the low incident energy range (≤ 30 eV) where the absorption effects are absent or small. In order to treat the absorption effects, those methods of close-coupling nature would require all discrete and continuum open channels to be included in the open-channel P space, which are still computationally unfeasible. In view of the difficulties, the use of the model absorption potential seems to be presently the only practical manner to

account for absorption effects into electron-molecule scattering calculations. Several model absorption potentials have been proposed and used, but version 3 of the quasifree scattering model (QFSM) proposed by Staszewska *et al.* [40], and lately modified by Jain and Baluja [41], has shown to yield cross sections in better agreement when compared with experiments. We have chosen the latter to account for the absorption component of the electron-radical interaction potential. The absorption potential V_{ab} in Eq. (1) is given by

$$V_{ab}(\vec{r}) = -\rho(\vec{r})(T_L/2)^{1/2}(8\pi/5k^2k_F^3)H(\alpha + \beta - k_F^2)(A + B + C), \quad (2)$$

where

$$T_L = k^2 - V^{SEP}, \quad (3)$$

$$A = 5k_F^3/(\alpha - k_F^2), \quad (4)$$

$$B = -k_F^3[5(k^2 - \beta) + 2k_F^2]/(k^2 - \beta)^2, \quad (5)$$

and

$$C = 2H(\alpha + \beta - k^2) \frac{(\alpha + \beta - k^2)^{5/2}}{(k^2 - \beta)^2}. \quad (6)$$

In Eqs. (2)–(6), k^2 is the energy (in Rydbergs) of the incident electron, k_F the Fermi momentum, and $\rho(\vec{r})$ the local electronic density of the target. $H(x)$ is a Heaviside function defined by $H(x)=1$ for $x \geq 0$ and $H(x)=0$ for $x < 0$. In the modified QFSM version 3 [41],

$$\alpha(\vec{r}, E) = k_F^2 + 2(\Delta - I) - V^{SEP}, \quad (7)$$

and

$$\beta(\vec{r}, E) = k_F^2 + 2(I - \Delta) - V^{SEP}, \quad (8)$$

where Δ is the average excitation energy and I is the ionization potential. In the original version of Staszewska *et al.*, V^{SEP} present in Eqs. (3), (7), and (8) are replaced by the static-exchange potential V^{SE} in the calculation of the local velocity of the scattering electron. In the present study, the experimental first ionization potential (13.17 eV) [42] is used as the average excitation energy as suggested by Jain and Baluja [41].

Since OH is an open-shell target, the coupling of the incident electron with the unpaired 1π electron of the target leads to two spin-specific scattering channels, namely, the singlet ($S=0$) and triplet ($S=1$) couplings. The main difference between the singlet and triplet scattering channels would reflect on the treatment of the electron-exchange term in the potential operator. On the other hand, contributions such as V_{st} , V_{cp} , and V_{ab} are calculated in the present study using the target electronic density and some molecular properties such as ionization potential, dipole polarizability, etc. Thus they are not explicitly dependent on the spin couplings.

Further, the spin-specific Lippmann-Schwinger (LS) equation is solved using the SVIM. In principle, this scattering equation for elastic e^- -OH scattering should be solved with the full complex optical potential. Nevertheless, a tremendous computational effort would be required, particu-

larly due to the large number of coupled equations involved, which makes such calculations practically prohibitive. On the other hand, our calculation has revealed that the magnitude of the imaginary part (absorption) of the optical potential is considerably smaller than its real counterpart. So, it can be treated as a perturbation. Therefore, in the present study, the LS scattering equations are solved using SVIM considering only the real part of the optical potential. In the SVIM calculations, the continuum wave functions are single-center expanded as

$$\chi_k^{\pm,S}(\vec{r}) = (2/\pi)^{1/2} \sum_{lm} \frac{(i)^l}{k} \chi_{klm}^{\pm,S}(\vec{r}) Y_{lm}(\hat{k}), \quad (9)$$

where the superscripts (+) and (-) denote the incoming-wave and outgoing-wave boundary conditions, respectively, S is the total spin of the (electron + target) system, and $Y_{lm}(\hat{k})$ are the usual spherical harmonics. The absorption part of the T matrix is calculated via the DWA as

$$T_{abs} = i \langle \chi_f^- | V_{ab} | \chi_i^+ \rangle. \quad (10)$$

In the present work, we have limited the partial-wave expansion of T -matrix elements up to $l_{max}=40$ and $m_{max}=17$. A Born-closure procedure is used to account for the contribution of higher partial-wave dipole components to scattering amplitudes. In order to avoid the divergent behavior of the DCS's in the forward direction, nuclear-rotational dynamics is treated explicitly.

The spin-specific rotational scattering amplitude is expressed as

$$f_{jm_j \leftarrow j_0 m_{j_0}}^S = \langle jm_j | f^S | j_0 m_{j_0} \rangle, \quad (11)$$

where $|jm_j\rangle$ are the rigid-rotor wave functions and $f^{(S)}$ the spin-specific fixed-nuclear electron scattering amplitude in the laboratory frame (LF). Accordingly, the spin-specific DCS's for the rotational excitation from an initial level j_0 to a final level j is given by

$$\left(\frac{d\sigma}{d\Omega} \right)^S (j \leftarrow j_0) = \frac{k_f}{k_0} \frac{1}{(2j_0 + 1)} \sum_{m_j m_{j_0}} |f_{jm_j \leftarrow j_0 m_{j_0}}^S|^2, \quad (12)$$

where k_f and k_0 are the final and initial linear momenta of the scattering electron, respectively.

Moreover, the spin-specific rotationally unresolved DCS's for elastic e^- -OH scattering are calculated via a summation of rotationally resolved DCS's,

$$\left(\frac{d\sigma}{d\Omega} \right)^S = \sum_{j=0} \left(\frac{d\sigma}{d\Omega} \right)^S (j \leftarrow j_0). \quad (13)$$

Finally, the spin-average DCS's for elastic e^- -OH scattering is calculated using the statistical weight for singlet (1/4) and triplet (3/4) scattering channels, as

$$\left(\frac{d\sigma}{d\Omega} \right) = \frac{1}{4} \left[3 \left(\frac{d\sigma}{d\Omega} \right)^{S=1} + \left(\frac{d\sigma}{d\Omega} \right)^{S=0} \right]. \quad (14)$$

In the present study, a standard basis set of Dunning [43] augmented by three s ($\alpha=0.05, 0.02$, and 0.005), one p ($\alpha=0.04$), and three d ($\alpha=1.7, 0.85$, and 0.34) uncontracted

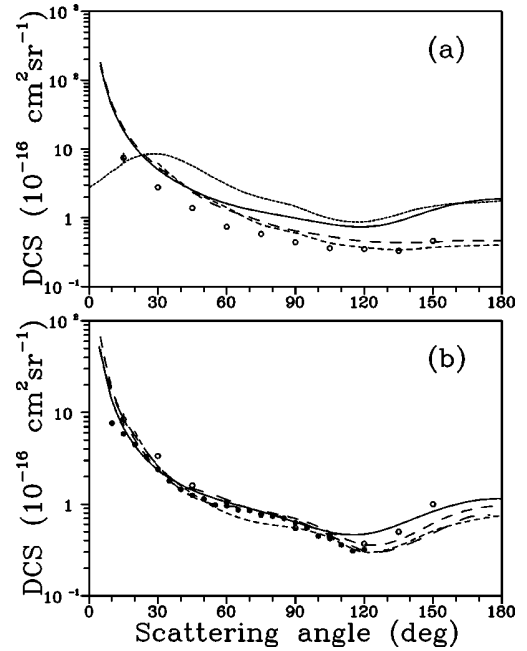


FIG. 1. DCS's for elastic e^- -OH scattering at (a) 2 eV and (b) 6 eV. Solid line, present rotationally summed results; dotted line, the R -matrix DCS's at 1.58 eV; the calculated results for e^- -H₂O scattering are of: short-dashed line, Rescigno and Lengsfeld [46]; dashed line, Machado *et al.* [47]; long-dashed line, Gianturco [45]. The experimental results for e^- -H₂O scattering are of: open circles, Shyn and Cho [52]; full circles, Johnstone and Newell [53]. The quoted experimental uncertainties of the DCS's vary from 9% to 15%. Representative error bars of some selected data are also shown.

functions for oxygen atom and a Gaussian basis set of Huzinaga [44] augmented by three p ($\alpha=1.0, 0.5$, and 0.1) uncontracted functions for the hydrogen atom are used for the calculation of the SCF wave function of the target. At the experimental equilibrium geometry of the ground-state OH ($R=1.830$ a.u.) [42], this basis set yielded the dipole moment of 1.789 D, which agrees reasonably well with the experimental value of 1.688 D [42].

III. RESULTS AND DISCUSSION

In Figs. 1–4 we show our calculated spin-averaged DCS's (rotationally summed) for elastic e^- -OH scattering in the 2–500-eV energy range. The R -matrix DCS's, calculated by Chen and Morgan [26] at the single incident energy of 1.58 eV, are shown in Fig. 1(a) to be compared with our results of 2 eV. Since no experimental or other theoretical results of DCS's for this target are available in the literature, we also use the existing calculated [45–49] and measured [50–53] results for elastic e^- -H₂O collisions to compare with our data. A similar procedure has already been adopted in some previous studies for CH [6] and SiH [7] radicals. Thus we expect that it may provide some insight of the dynamics for elastic e^- -OH collision. It is interesting to see, in Fig. 1(a), that there is a fairly good agreement between our calculated results at 2 eV and the R -matrix DCS's at 1.58 eV at

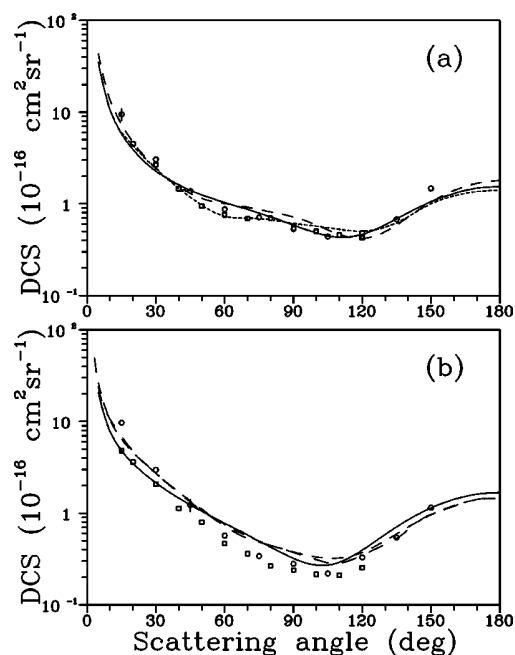


FIG. 2. Same as Fig. 1 except at (a) 10 eV and (b) 20 eV. Open squares, experimental DCS's for e^- -H₂O scattering of Danjo and Nishimura [50].

the intermediate and large scattering angles. However, the R -matrix results present a deep falloff at small scattering angles, due to the nonconvergent partial-wave expansions. In addition, one notes that at 2 eV, there is a good agreement between the present calculated results for OH and those calculated for H₂O, particularly at small scattering angles. It is

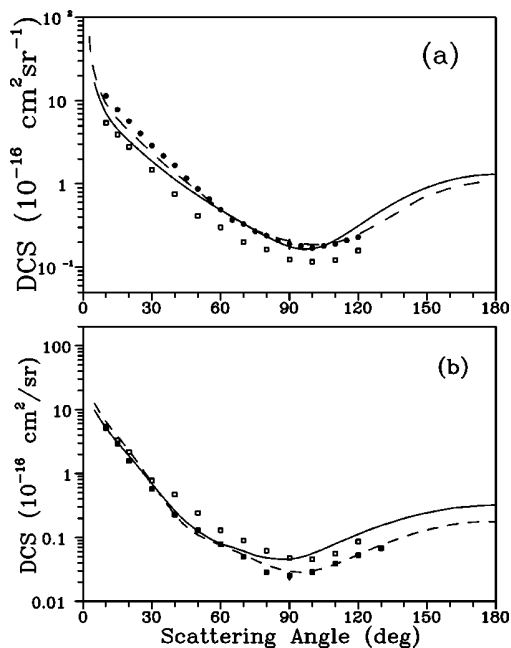


FIG. 3. Same as Fig. 1 except at (a) 30 eV and (b) 100 eV. Full squares, experimental data for e^- -H₂O scattering of Katase *et al.* [51]; dashed line, calculated results for H₂O of Machado [49].

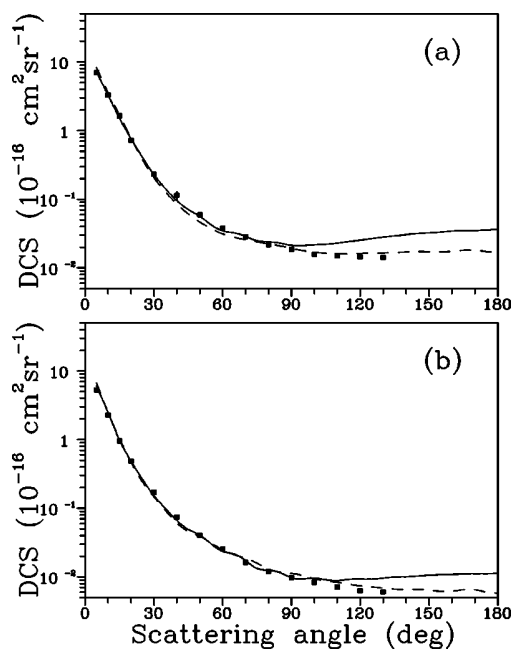


FIG. 4. Same as Fig. 3, except at (a) 300 eV and (b) 500 eV.

well known that at such a low incident energy, the long-range interaction potentials of either permanent and/or induced natures are dominant in the collisional dynamics. The fact that the similarity of the permanent dipole of the targets, 1.68 D for OH and 1.85 D for H₂O [42], may explain this good agreement, despite the larger difference in the average polarizability, 7.4 a.u. for OH and 10.5 a.u. for H₂O [39]. It is due to the fact that polarization effects are less important for strongly polar targets. At higher incident energies, remarkable similarity between the calculated DCS's for electron scattering by OH and H₂O are more apparent. This good agreement clearly indicates that the electron interaction with the heavier oxygen atom is dominant for both targets and the loss of one hydrogen atom in OH is not relevant. Also, the good agreement between the calculated and experimental DCS's for e^- -H₂O scattering may provide some indications of the reliability of the present study.

In Figs. 5(a) and 5(b) we show our spin-averaged ICS's and MTCS's for elastic e^- -OH collisions, respectively, calculated in the 1–500-eV range. Again, comparison is made with the calculated [45–49] and experimental [50–52] results for e^- -H₂O scattering. In general, ICS's and MTCS's for elastic electron scattering by both targets agree well with each other, which again reinforces that the electron-oxygen atom interaction is dominant. Also, a broad enhancement centered at around 13 eV is seen in both ICS's and MTCS's. In fact, this enhancement is a consequence of the occurrence of weak resonances in $1,3\Sigma$ and $1,3\Pi$ scattering channels. A similar resonance feature is also seen, at about the same energies, in e^- -H₂O scattering.

In Fig. 6(a) we show our spin-averaged TCS's for e^- -OH collisions calculated in the 1–500-eV range. The TCS's for this radical calculated by Joshipura *et al.* [5] using the additivity rule as well as calculated [54] and experimental [55–58] TCS's for e^- -H₂O scattering available in the lit-

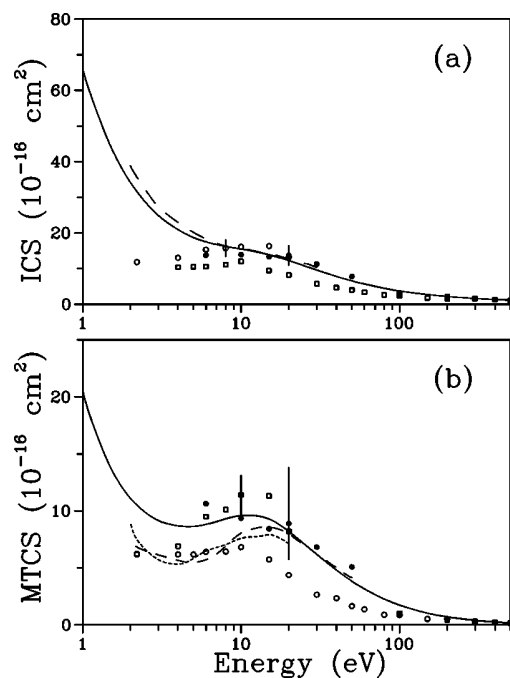


FIG. 5. (a) ICS's and (b) MTCS's for elastic e^- -OH scattering. Solid line, present rotationally summed results; the calculated results for e^- -H₂O scattering are of: short-dashed line, Rescigno and Lengsfeld [46]; dashed line, Machado *et al.* [47]; long-dashed line, Gianturco [45]. The experimental results for e^- -H₂O scattering are of: open squares, Danjo and Nishimura [50]; open circles, Shyn and Cho [52]; full squares, Katase *et al.* [51]; full circles, Johnstone and Newell [53]. The quoted experimental uncertainties of the ICS's vary from 13% to 22% and those of the MTCS's are from 13% to 55%. Representative error bars of some selected data are also shown.

erature are shown for comparison. In general, there is a good agreement between the present data and those of Joshipura *et al.* However, the calculated TCS of Jain [54] for e^- -H₂O scattering lie systematically above our data. On the other hand, there is a significant discrepancy among the experimental TCS's for e^- -H₂O scattering, particularly at the low incident energies. It is seen that the present calculated data agree better with those of Sokolov and Sokolova [55] at low energies and with those of Sueoka *et al.* [56] at high incident energies. In Fig. 6(b) we show our spin-averaged TACS's for e^- -OH collisions calculated in the 10–500-eV range. The TACS's calculated by Joshipura *et al.* [5] using the additivity

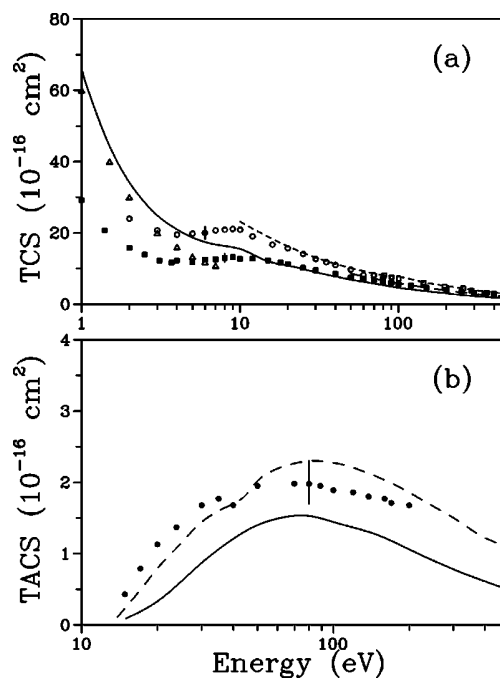


FIG. 6. (a) TCS's and (b) TACS's for e^- -OH scattering. Solid line, present results; dashed line, the calculated results for e^- -OH scattering of Joshipura *et al.* [5]; short-dashed line, the calculated results for e^- -H₂O scattering of Jain [54]; full circles, the experimental TICS for OH of Tanovsky *et al.* [25]. The experimental TCS's for e^- -H₂O scattering are of: open triangles, Sokolov and Sokolova [55]; full squares, Sueoka *et al.* [56]; open circles, Szmytkowski [57]; open squares, Zecca *et al.* [58]. The quoted experimental uncertainties of the TCS's vary from 1% to 10% and those of the TICS's are 15%. Representative error bars of some selected data are also shown.

rule as well as the experimental TICS's of Tanovsky *et al.* [25] for this radical are also shown for comparison. In general, there is a good qualitative agreement among the calculated and experimental data. Quantitatively, the agreement between the present TACS's and the experimental TICS's is fair.

ACKNOWLEDGMENTS

This work was partially supported by the Brazilian agencies FAPESP, CNPq, and CAPES.

[1] S. Trajmar, D. F. Register, and A. Chutjian, *Phys. Rep.* **97**, 219 (1983).
 [2] J. Hahn and C. Junge, *Z. Naturforsch. A* **32**, 190 (1977).
 [3] W. Wang and N. D. Sze, *Nature (London)* **286**, 589 (1980).
 [4] K. N. Joshipura and M. Vinodkumar, *Phys. Lett. A* **224**, 361 (1997).
 [5] K. N. Joshipura, M. Vinodkumar, and P. M. Patel, *J. Phys. B* **34**, 509 (2000).

[6] M.-T. Lee, M. F. Lima, A. M. C. Sobrinho, and I. Iga, *J. Phys. B* **35**, 2437 (2002).
 [7] M.-T. Lee, M. F. Lima, A. M. C. Sobrinho, and I. Iga, *Phys. Rev. A* **66**, 062703 (2002).
 [8] M.-T. Lee, I. Iga, L. M. Brescansin, L. E. Machado, and F. B. C. Machado, *Phys. Rev. A* **66**, 012720 (2002).
 [9] S. C. Brown, *Electron-Molecule Scattering* (Wiley, New York, 1979).

- [10] R. K. Jane, in *Atomic and Plasma-Material Interaction Processes in Controlled Thermonuclear Fusion*, edited by R. K. Janev and H. W. Drawin (Elsevier, Amsterdam, 1993), p. 27.
- [11] J. J. Perry, Y. H. Kim, J. L. Fox, and H. S. Porter, *J. Geophys. Res.* **104**, 16541 (1999).
- [12] G. Heit, A. Neuner, P. Y. Saugy, and A. M. Braun, *J. Phys. Chem. A* **102**, 5551 (1998).
- [13] D. J. Creasey, G. E. Evans, D. E. Heard, and J. D. Lee, *J. Geophys. Res.*, [Atmos.] **108**, 4475 (2003).
- [14] M. Vrtacnik and K. Voda, *Chemosphere* **52**, 1689 (2003).
- [15] X. R. Ren, H. Harder, M. Martines, R. L. Leshner, A. Olinger, and J. B. Simpas, W. H. Brune, J. J. Schwab, K. L. Demerjian, Y. He, X. L. Zhou, and H. G. Gao, *Atmos. Environ.* **37**, 3639 (2003).
- [16] R. Atkinson, *Atmos. Chem. Phys.* **3**, 2233 (2003).
- [17] K. E. S. Ford, D. A. Neufeld, P. F. Goldsmith, and G. J. Melnick, *Astrophys. J.* **589**, 430 (2003).
- [18] J. P. Morgenthaler, W. M. Harris, F. L. Roesler, F. Scherb, C. M. Anderson, N. E. Doane, and R. J. Oliverson, *Earth, Moon, Planets* **90(1-4)**, 77 (2002).
- [19] D. A. Neufeld, J. R. Stauffer, E. A. Bergin, S. C. Kleiner, B. M. Patten, Z. Wang, M. L. N. Ashby, G. Chin, N. R. Erickson, P. F. Goldsmith, M. Harwit, J. E. Howe, D. G. Koch, R. Plume, R. Schieder, R. L. Snell, V. Tolls, G. Winnewisser, Y. F. Zhang, and G. J. Melnick, *Astrophys. J. Lett.* **539**, L151 (2000).
- [20] E. Fernandes, S. A. Toste, J. L. F. C. Lima, and S. J. Reis, *Free Radic Biol. Med.* **35**, 1008 (2003).
- [21] S. S. Leonard, C. Xia, B. H. Jiang, B. Stinefelt, H. Klandorf, G. K. Harris, and X. L. Shi, *Biochem. Biophys. Res. Commun.* **309**, 1017 (2003).
- [22] I. P. Kumar, S. V. S. Rana, N. Samanta, and H. C. Goel, *J. Pharm. Pharmacol.* **55**, 1267 (2003).
- [23] H. B. An, J. Xie, J. Q. Zhao, and Z. S. Li, *Free Radical Res.* **37**, 1107 (2003).
- [24] A. Katase, K. Ishibashi, Y. Matsumoto, T. Sakae, S. Maezono, E. Murakami, K. Watanabe, and H. Maki, *J. Phys. B* **19**, 2715 (1986).
- [25] V. Tanovsky, H. Deutsch, and K. Becker, *J. Chem. Phys.* **109**, 932 (1998).
- [26] X. Chen and L. A. Morgan, *J. Phys. B* **30**, 3709 (1997).
- [27] R. R. Lucchese, G. Raseev, and V. McKoy, *Phys. Rev. A* **25**, 2572 (1982).
- [28] L. Mu-Tao, L. M. Brescansin, M. A. P. Lima, L. E. Machado, and E. P. Leal, *J. Phys. B* **23**, 4331 (1990).
- [29] A. W. Fliflet and V. McKoy, *Phys. Rev. A* **21**, 1863 (1980).
- [30] M.-T. Lee and V. McKoy, *Phys. Rev. A* **28**, 697 (1983).
- [31] M.-T. Lee, S. Michelin, L. E. Machado, and L. M. Brescansin, *J. Phys. B* **26**, L203 (1993).
- [32] M.-T. Lee, I. Iga, L. E. Machado, and L. M. Brescansin, *Phys. Rev. A* **62**, 062710 (2000).
- [33] M.-T. Lee and I. Iga, *J. Phys. B* **32**, 453 (1999).
- [34] I. Iga, M. G. P. Homem, K. T. Mazon, and M.-T. Lee, *J. Phys. B* **32**, 4373 (1999).
- [35] S. E. Michelin, T. Kroin, I. Iga, M. G. P. Homem, and M.-T. Lee, *J. Phys. B* **33**, 3293 (2000).
- [36] N. T. Padial and D. W. Norcross, *Phys. Rev. A* **29**, 1742 (1984).
- [37] A. Faure, J. D. Gorfinkiel, and J. Tennyson, *J. Phys. B* **37**, 801 (2004).
- [38] C. S. Trevisan, A. E. Oral, and T. N. Rescigno, *Phys. Rev. A* **68**, 062707 (2003).
- [39] C. Winstead and V. McKoy, *J. Chem. Phys.* **116**, 1380 (2002).
- [40] G. Staszewska, D. W. Schwenke, and D. G. Truhlar, *Phys. Rev. A* **29**, 3078 (1984).
- [41] A. Jain and K. L. Baluja, *Phys. Rev. A* **45**, 202 (1992).
- [42] D. R. Lide, *CRC Handbook of Chemistry and Physics* (Chemical Rubber Company, Boca Raton, FL, 1993).
- [43] T. H. Dunning, *J. Chem. Phys.* **55**, 716 (1971).
- [44] S. Huzinaga, *J. Chem. Phys.* **42**, 1293 (1965).
- [45] F. A. Gianturco, *J. Phys. B* **24**, 3837 (1991).
- [46] T. Rescigno and B. M. Lengsfeld, *Z. Phys. D: At., Mol. Clusters* **24**, 117 (1992).
- [47] L. E. Machado, M.-T. Lee, L. M. Brescansin, M. A. P. Lima, and V. McKoy, *J. Phys. B* **28**, 476 (1995).
- [48] M. T. N. Varella, M. H. F. Bettega, M. A. P. Lima, and L. G. Ferreira, *J. Chem. Phys.* **111**, 6369 (1999).
- [49] L. E. Machado (private communication).
- [50] A. Danjo and H. Nishimura, *J. Phys. Soc. Jpn.* **54**, 1224 (1985).
- [51] A. Katase, K. Ishibashi, Y. Matsumoto, T. Sakae, S. Maezono, E. Murakami, K. Watanabe, and H. Maki, *J. Phys. B* **19**, 2715 (1986).
- [52] T. W. Shyn and S. Y. Cho, *Phys. Rev. A* **36**, 5138 (1987).
- [53] W. M. Johnstone and W. R. Newell, *J. Phys. B* **24**, 3663 (1991).
- [54] A. Jain, *J. Phys. B* **21**, 905 (1988).
- [55] V. F. Sokolov and Y. A. Sokolova, *Sov. Tech. Phys. Lett.* **7**, 268 (1981).
- [56] O. Sueoka, S. Mori, and Y. Katayama, *J. Phys. B* **19**, L373 (1986).
- [57] Cz. Szmytkowski, *Chem. Phys. Lett.* **136**, 363 (1987).
- [58] A. Zecca, G. Karwasz, S. Oss, R. Grisenti, and R. S. Brusa, *J. Phys. B* **20**, L133 (1987).